

# A Monadic Framework for Bidirectional Programming

## Motivation

- ▶ Two ways to run a program: avoids code duplication.
- ▶ Monads have expressiveness and readability: they might make bidirectional programming easier.

## Three types of bidir. transformations (BX)

- ▶ An *invertible parser* can be turned around into a printer.

```
data InvParser x a = InvParser
  { parse :: String -> (String, a)
  , print :: x -> (String, a) }
```

- ▶ A *lens* lifts functions  $(a \rightarrow x)$  into updates on  $s$ .

```
data Lens s x a = Lens
  { get :: s -> a
  , set :: x -> s -> (s, a) }
```

- ▶ A *generable set* consists of a random generator and a membership function.

```
data GSet x a = GSet
  { generate :: Gen (Maybe a)
  , predicate :: x -> Maybe a }
```

## Monadic bidirectional transformations

- ▶ A pair of **reader** and **writer** transformations.
- ▶ Parameterized by an *input* type  $x$  and an *output* type  $a$ .

```
data MBX r w x a = MBX
  { reader :: r a
  , writer :: x -> w a }
instance (Monad r, Monad w) => Monad (MBX r w x)
```

## Common interpretation

- ▶ Readers map a **source**  $s$  to some **view**  $a$ .
- ▶ Writers take a value  $x$  containing a view  $a$ , and instantiate a **partially defined source**  $s'$  such that reading from any complete instantiation yields back  $a$ .

A printer “writes” a string by incrementally instantiating an unknown prefix  $(\_)$ . The final string is obtained by substituting the last unknown with the empty string  $""$ .

```
(_) > ("1" ++ _) > ("1 0" ++ _) > ("1 0 -" ++ _)
> ... > ("1 0 - - 2 - 3 - -" ++ _)
```

- ▶ We expect that every written view can be read back. This is analogous to the *PutGet* lens law.

## References

- ▶ *Combinators for bidirectional tree transformations: A linguistic approach to the view update problem.* Foster et al. (POPL'05)
- ▶ *Invertible Syntax Descriptions: Unifying Parsing and Pretty Printing.* Rendel and Ostermann. (Haskell'10)
- ▶ *Applicative bidirectional programming with lenses.* Matsuda and Wang. (ICFP'15)
- ▶ *Beginner's Luck: A Language for Property-Based Generators.* Lampropoulos et al. (POPL'17)

## Monadic profunctors (MP)

- ▶ MBXs are **monadic profunctors**.
- ▶ A monadic profunctor is a *monad*,  
 $\text{return} :: a \rightarrow p \times a$   
 $(\gg=) :: p \times a \rightarrow (a \rightarrow p \times b) \rightarrow p \times b$
- ▶ also a *contravariant functor (cofunctor)*,  
 $(=.) :: (y \rightarrow x) \rightarrow p \times a \rightarrow p \times y \times a$
- ▶ such that  $(f =.)$  is a *monad morphism* for all  $f$ .  
 $> f =. \text{return } a = \text{return } a$   
 $> f =. ( \text{ma} \gg= (\lambda a \rightarrow \text{amb } a) )$   
 $= (f =. \text{ma}) \gg= (\lambda a \rightarrow f =. \text{amb } a)$

## Example: Parsing and printing trees

In the definition of a MBX like tree, every action is annotated with its “location” in the final result. Erasing these annotations in gray below reveals the code of a parser.

```
word :: InvParser String String
data Tree = L | Node Integer Tree Tree

tree :: InvParser Tree Tree
tree = do
  w <- firstWord =. word
  case w of
    "-" -> return L
    _   -> do l <- nodeLeft =. tree
              r <- nodeRight =. tree
              return (Node (read w) l r)
  where firstWord L = "-"
        firstWord (Node v _ _) = show v
```

```
example = Node 1 (Node 0 L L)
              (Node 2 L (Node 3 L L))
output  = "1 0 - - 2 - 3 - -"
```

- $> \text{runPrinter } (\text{print tree example}) = \text{output}$
  - $> \text{runParser } (\text{parse tree}) \text{ output} = \text{example}$
- A more realistic example of invertible parser:  
<https://github.com/Lysxia/unparse-attoparsec>.

## BX xor MP

- ▶ BX but not MP: bijections.
- ▶ MP but not BX: “Profunctor HOAS”.  
(<https://www.schoolofhaskell.com/user/edwardk/phoas>)

## Future directions

- ▶ Refine MPs, e.g., as cofunctors in a category of arrows.
- ▶ Interpretation still needs adjustment for **GSet**.
- ▶ How to derive reader from writer (or conversely).